## inorganic compounds

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## $\boldsymbol{\alpha}-\mathrm{Ba}_{2} \mathrm{P}_{2} \mathrm{O}_{7}$

Driss Zakaria, ${ }^{\text {a }}$ Fatima Erragh, ${ }^{\text {a }}$ Abdelghani Oudahmane, ${ }^{\text {b }}$ Malika El-Ghozzi ${ }^{\text {b }}$ and Daniel Avignant ${ }^{\text {b* }}$<br>${ }^{\text {a }}$ Laboratoire de Physico-Chimie des Matériaux, Université Chouaib Doukkali, Faculté des Sciences BP 20, 24000 El Jadida, Morocco, and ${ }^{\text {b }}$ Université Blaise Pascal, Laboratoire des Matériaux Inorganiques, UMR CNRS 6002, 24 Avenue des Landais, 63177 Aubière, France<br>Correspondence e-mail: daniel.avignant@univ-bpclermont.fr

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Key indicators: single-crystal X-ray study; $T=296 \mathrm{~K}$; mean $\sigma(\mathrm{P}-\mathrm{O})=0.001 \AA$; $R$ factor $=0.021 ; w R$ factor $=0.046$; data-to-parameter ratio $=69.4$.

Single crystals of $\alpha-\mathrm{Ba}_{2} \mathrm{P}_{2} \mathrm{O}_{7}$, dibarium diphosphate, were obtained by solid-state reaction. The orthorhombic structure is isotypic with $\alpha-\mathrm{Sr}_{2} \mathrm{P}_{2} \mathrm{O}_{7}$ and is the second polymorph obtained for this composition. The structure is built from two different $\mathrm{BaO}_{9}$ polyhedra (both with $m$ symmetry), with $\mathrm{Ba}-$ O distances in the ranges $2.7585(10)-3.0850$ (6) and 2.5794 (13)-2.9313 (4) $\AA$. These polyhedra are further linked by sharing corners along [010] and either edges or triangular faces perpendicularly to [010] to form the three-dimensional framework. This polyhedral linkage delimits large channels parallel to [010] where the $\mathrm{P}_{2} \mathrm{O}_{7}$ diphosphate anions are located. These groups (symmetry $m$ ) are characterized by a $\mathrm{P}-\mathrm{O}-\mathrm{P}$ angle of $131.52(9)^{\circ}$ and an eclipsed conformation. They are connected to the $\mathrm{BaO}_{9}$ polyhedra through edges and corners.

## Related literature

Besides crystals of the title compound, crystals of the hexagonal polymorph $\sigma-\mathrm{Ba}_{2} \mathrm{P}_{2} \mathrm{O}_{7}$ were obtained (ElBelghitti et al. 1995). For isotypic structures, see: Hagman et al. (1968); Grenier \& Masse (1977); Barbier \& Echard (1998). For closely related structures, see: Elmarzouki et al. (1995). For polymorphism in $\mathrm{Ba}_{2} \mathrm{P}_{2} \mathrm{O}_{7}$, see: McCauley \& Hummel (1968); Mehdi et al. (1977); Bian et al. (2004); Kokhanovskii (2004). For a review of the crystal chemistry of diphosphates, see: Durif (1995). For applications of alkaline earth diphosphates, see: Pang et al. (2009); Peng et al. (2010). For an independent refinement of the $\alpha-\mathrm{Ba}_{2} \mathrm{P}_{2} \mathrm{O}_{7}$ structure based on data from a hydrothermally grown crystal, see: Heyward et al. (2010).

## Experimental

## Crystal data

| $\mathrm{Ba}_{2} \mathrm{P}_{2} \mathrm{O}_{7}$ | Orthorhombic, Pnma |
| :--- | :--- |
| $M_{r}=448.62$ | $a=9.2875$ (1) |

$M_{r}=448.62$

| $b=5.6139(1) \AA$ | Mo $K \alpha$ radiation |
| :--- | :--- |
| $c=13.8064(1) \AA$ | $\mu=11.31 \mathrm{~mm}^{-1}$ |
| $V=719.85(2) \AA^{3}$ | $T=296 \mathrm{~K}$ |
| $Z=4$ | $0.26 \times 0.14 \times 0.14 \mathrm{~mm}$ |

Data collection
Bruker APEXII CCD
diffractometer
Absorption correction: multi-scan
(SADABS; Bruker, 2008)
$T_{\text {min }}=0.155, T_{\text {max }}=0.205$

## Refinement

$R\left[F^{2}>2 \sigma\left(F^{2}\right)\right]=0.021 \quad 62$ parameters
$w R\left(F^{2}\right)=0.046$
$S=1.07$
4304 reflections

18034 measured reflections 4304 independent reflections 3726 reflections with $I>2 \sigma(I)$ $R_{\text {int }}=0.028$
Mo $K \alpha$ radiation
$0.26 \times 0.14 \times 0.14 \mathrm{~mm}$
$\Delta \rho_{\text {max }}=1.59 \mathrm{e}_{\AA^{-3}}$
$\Delta \rho_{\text {min }}=-1.99 \mathrm{e}^{-3}$

Table 1
Selected bond lengths ( $\AA$ ).

| $\mathrm{Ba} 1-\mathrm{O} 3^{\mathrm{i}}$ | $2.7585(10)$ | $\mathrm{Ba} 2-\mathrm{O} 4^{\text {vi }}$ | $2.9313(4)$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{Ba} 1-\mathrm{O} 2^{\text {ii }}$ | $2.7591(10)$ | $\mathrm{P} 1-\mathrm{O} 5$ | $1.5067(13)$ |
| $\mathrm{Ba} 1-\mathrm{O} 4^{\text {iii }}$ | $2.7978(13)$ | $\mathrm{P} 1-\mathrm{O} 2^{\text {vii }}$ | $1.5208(11)$ |
| $\mathrm{Ba} 1-\mathrm{O} 2$ | $2.8392(10)$ | $\mathrm{P} 1-\mathrm{O} 2$ | $1.5208(11)$ |
| $\mathrm{Ba} 1-\mathrm{O} 5$ | $3.0850(6)$ | $\mathrm{P} 1-\mathrm{O} 1$ | $1.6148(13)$ |
| $\mathrm{Ba} 2-\mathrm{O} 5^{\text {iv }}$ | $2.5794(13)$ | $\mathrm{P} 2-\mathrm{O} 4^{\text {viii }}$ | $1.5175(13)$ |
| $\mathrm{Ba} 2-\mathrm{O} 3^{\text {ii }}$ | $2.7377(10)$ | $\mathrm{P} 2-\mathrm{O} 3^{\text {vii }}$ | $1.5236(11)$ |
| $\mathrm{Ba} 2-\mathrm{O} 2^{\text {iii }}$ | $2.8133(10)$ | $\mathrm{P} 2-\mathrm{O} 3$ | $1.5236(11)$ |
| $\mathrm{Ba} 2-\mathrm{O}^{\mathrm{v}}$ | $2.9094(10)$ | $\mathrm{P} 2-\mathrm{O} 1$ | $1.6012(14)$ |

Symmetry codes: (i) $x+\frac{1}{2}, y,-z+\frac{3}{2}$; (ii) $x+\frac{1}{2},-y+\frac{1}{2},-z+\frac{3}{2}$; (iii) $-x,-y,-z+1$; (iv) $-x+\frac{1}{2},-y, z-\frac{1}{2}$; (v) $-x-\frac{1}{2},-y, z-\frac{1}{2}$; (vi) $x+\frac{1}{2}, y+1,-z+\frac{1}{2}$; (vii) $x,-y-\frac{1}{2}, z$; (viii)
$x, y, z+1$.

Data collection: APEX2 (Bruker, 2008); cell refinement: SAINT (Bruker, 2008); data reduction: SAINT; program(s) used to solve structure: SHELXS97 (Sheldrick, 2008); program(s) used to refine structure: SHELXL97 (Sheldrick, 2008); molecular graphics: DIAMOND (Brandenburg, 1999) and ORTEP-3 for Windows (Farrugia, 1997); software used to prepare material for publication: SHELXTL (Sheldrick, 2008).

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Supplementary data and figures for this paper are available from the IUCr electronic archives (Reference: WM2413).

## References

Barbier, J. \& Echard, J. P. (1998). Acta Cryst. C54, IUC9800070.
Bian, J., Kim, D. W. \& Hong, K. S. (2004). Jpn. J. Appl. Phys. Part 1, 43, 35213525.

Brandenburg, K. (1999). DIAMOND. Crystal Impact GbR, Bonn, Germany.
Bruker (2008). SADABS, APEX2 and SAINT. Bruker AXS Inc., Madison, Wisconsin, USA.
Durif, A. (1995). Crystal Chemistry of Condensed Phosphates. New York, London: Plenum Press
ElBelghitti, A. A., Elmarzouki, A., Boukhari, A. \& Holt, E. M. (1995). Acta Cryst. C51, 1478-1480.
Elmarzouki, A., Boukhari, A., Holt, E. M. \& Berrada, A. (1995). J. Alloys Compd. 227, 125-130.
Farrugia, L. J. (1997). J. Appl. Cryst. 30, 565.
Grenier, J. C. \& Masse, R. (1977). Bull. Soc. Fr. Miner. Cristallogr. 92, 91-92.
Hagman, L. O., Jansson, I. \& Magneli, C. (1968). Acta Chem. Scand. 22, 14191429.

Heyward, C., Mann, M. \& Kolis, J. (2010). Acta Cryst. E66. In the press.
Kokhanovskii, V. (2004). Zh. Neorg. Khim. 49, 511-517.

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McCauley, R. A. \& Hummel, F. A. (1968). Trans. Br. Ceram. Soc. 67, 619628.

Mehdi, S., Raza Hussain, M. \& Rama Rao, B. (1977). Indian J. Chem. Sect. A, 15, 820-821.

Pang, R., Li, C., Shi, L. \& Su, Q. (2009). J. Phys. Chem. Solids, 70, 303-306. Peng, M., Sprenger, B., Schmidt, A., Schwefel, H. G. L. \& Wondraczek, L. (2010). Opt. Express, 18, 12852-12863.

Sheldrick, G. M. (2008). Acta Cryst. A64, 112-122.

## supplementary materials

## $\boldsymbol{\alpha}-\mathrm{Ba}_{2} \mathrm{P}_{2} \mathrm{O}_{7}$

D. Zakaria, F. Erragh, A. Oudahmane, M. El-Ghozzi and D. Avignant

## Comment

Due to their potential applications as optical materials (Pang et al., 2009, Peng et al., 2010), alkaline earth diphosphates exhibit at the present time a growing interest. Since the optical properties are strongly related to the crystal structure, the study of polymorphism in these materials is worth investigating. Besides the hexagonal form $\sigma$ - $\mathrm{Ba}_{2} \mathrm{P}_{2} \mathrm{O}_{7}$ described by ElBelghitti et al. (1995), the title compound is the second polymorph for this composition obtained in the form of single-crystals. The orthorhombic title compound $\alpha-\mathrm{Ba}_{2} \mathrm{P}_{2} \mathrm{O}_{7}$ is isotypic with $\alpha-\mathrm{Sr}_{2} \mathrm{P}_{2} \mathrm{O}_{7}$ (Hagman et al. 1968; Grenier \& Masse, 1977; Barbier \& Echard, 1998) and closely related to $\mathrm{BaPbP}_{2} \mathrm{O}_{7}$ (Elmarzouki et al., 1995). The existence of this polymorph has previously been mentioned by Durif (1995) and several other authors (McCauley \& Hummel, 1968; Mehdi et al., 1977; Bian et al., 2004; Kokhanovskii, 2004).

The structure of the $\alpha$-polymorph is built up from two different $\mathrm{BaO}_{9}$ polyhedra with $\mathrm{Ba}-\mathrm{O}$ distances ranging from 2.7585 (10) $\AA$ to 3.0850 (6) $\AA$ and from 2.5794 (13) $\AA$ to 2.9313 (4) $\AA$, respectively. Figure 1 displays details of these coordination polyhedra as well as their linkage by corners, edges or triangular faces to form the three-dimensional framework. This polyhedral linkage delimits large channels parallel to [010] where the $\mathrm{P}_{2} \mathrm{O}_{7}$ diphosphate groups are located (Fig. 2). These groups (symmetry $m$ ) are characterized by a $\mathrm{P}-\mathrm{O}-\mathrm{P}$ angle of 131.52 (9) ${ }^{\circ}$ and an eclipsed conformation. They are connected to the $\mathrm{BaO}_{9}$ polyhedra through edges and corners. Each oxygen atom of the $\mathrm{P}_{2} \mathrm{O}_{7}$ groups, apart from the O 1 bridging oxygen, is bonded to three Ba atoms and one phosphorus atom. During the anisotropic refinement of the displacement parameters of the isotypic $\alpha-\mathrm{Sr}_{2} \mathrm{P}_{2} \mathrm{O}_{7}$ structure (Barbier \& Echard, 1998), the authors observed a very strong anisotropy along the $b$ direction for both O 5 and O 1 atoms located in the ( 010 ) mirror plane and interpreted this phenomenon as a possible atomic-scale disorder associated with the local loss of mirror symmetry resulting in a non-centrosymmetric structural arrangement. Such an outstanding feature is still present in our anisotropic structure refinement, although the amplitudes of the atomic displacement parameters are significantly lower, especially for the $U_{22}$ component of the O 5 atom. If the strong anisotropy of the O 1 atom is perfectly understandable because of its bridging role, that of the O 5 atom strongly bonded to two Ba 1 atoms at 3.0850 (6) $\AA$, one Ba 2 atom at 2.5794 (13) $\AA$ and one P 1 atom at 1.5067 (13) $\AA$ is more surprising. However, due to the relative homogeneity of the values of the isotropic displacement parameters of all oxygen atoms, it does not seem necessary to envisage any atomic-scale disorder for the O 5 atom in the present case.

Simultaneous with our refinement, an independent study of the $\alpha-\mathrm{Ba}_{2} \mathrm{P}_{2} \mathrm{O}_{7}$ structure from a hydrothermally grown crystal was reported by Heyward et al. (2010). The results of both refinements in terms of geometric parameters are the same within the threefold standard deviation.

## Experimental

Single crystals of the title compound have been obtained during the study of the phase relationships in the ternary system $\mathrm{Na}_{2} \mathrm{O}-\mathrm{BaO}-\mathrm{P}_{2} \mathrm{O}_{5}$. They were synthesized in the solid state by reacting $\mathrm{Na}_{2} \mathrm{CO}_{3}, \mathrm{BaCO}_{3}$ and $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{HPO}_{4}$ in a platinum crucible. A mixture of these reagents taken in the molar ratio 1:1:2 was carefully ground in an agate mortar and successively

## supplementary materials

heated at $373 \mathrm{~K}, 573 \mathrm{~K}$ and 773 K for 24 h at each temperature. After a new grinding, the reacting mixture was submitted to a final heat treatment at 973 K for 2 days followed by a slow cooling to room temperature at the rate of $5 \mathrm{~K} \mathrm{~h}^{-1}$. After an abundant washing of the batch with hot water, single crystals of the title compound could have been extracted.

## Refinement

The highest residual peak in the final difference Fourier map was located $0.56 \AA$ from atom Ba 1 and the deepest hole was located $0.31 \AA$ from atom Ba 2 .

## Figures



Fig. 1. View of the $\mathrm{BaO}_{9}$ polyhedra linkage in $\alpha-\mathrm{Ba}_{2} \mathrm{P}_{2} \mathrm{O}_{7}$. Displacement ellipsoids are drawn at the $50 \%$ probability level. Symmetry codes: (i) $x+1 / 2, y,-z+3 / 2$; (ii) $x+1 / 2,-y+1 / 2,-z$ $+3 / 2$; (iii) $-x,-y,-z+1$; (iv) $x,-y+1 / 2, z$; (v) $x, y+1, z$; (vii) $-x, y+1 / 2,-z+1$; (viii) $-x-1 /$ $2,-y, z-1 / 2$; (ix) $-x-1 / 2, y+1 / 2, z-1 / 2$; (x) $x+1 / 2, y+1,-z+1 / 2$; (xi) $x+1 / 2, y,-z+1 / 2$; (xii) $x+1 / 2, y+1,-z+3 / 2$; (xiii) $x,-y-1 / 2, z$; (xiv) $x, y, z+1$; (xv) $-x-1 / 2,-y, z+1 / 2$; (xvi) $x-1 / 2, y,-z+3 / 2$; (xviii) $x, y, z-1 ;-z+1 / 2$; (xx) $x-1 / 2, y,-z+1 / 2 ;$ (xxi) $-x+1 / 2,-y, z+1 / 2$; (xxii) $x, y-1, z$;

Fig. 2. Projection of the $\alpha-\mathrm{Ba}_{2} \mathrm{P}_{2} \mathrm{O}_{7}$ structure along [010] showing the connections between the $\mathrm{P}_{2} \mathrm{O}_{7}$ diphosphate groups and the three-dimensional framework of the $\mathrm{BaO}_{9}$ polyhedra.

## dibarium diphosphate

## Crystal data

$\mathrm{Ba}_{2} \mathrm{P}_{2} \mathrm{O}_{7}$
$F(000)=792$
$M_{r}=448.62$
Orthorhombic, Pnma
Hall symbol: -P 2ac 2n
$a=9.2875$ (1) $\AA$
$b=5.6139(1) \AA$
$c=13.8064(1) \AA$
$V=719.85(2) \AA^{3}$
$Z=4$
$D_{\mathrm{x}}=4.139 \mathrm{Mg} \mathrm{m}^{-3}$
Mo $K \alpha$ radiation, $\lambda=0.71073 \AA$
Cell parameters from 7790 reflections
$\theta=3.7-52.2^{\circ}$
$\mu=11.31 \mathrm{~mm}^{-1}$
$T=296 \mathrm{~K}$
Hexagonal prism, colourless
$0.26 \times 0.14 \times 0.14 \mathrm{~mm}$

## Data collection

Bruker APEXII CCD
diffractometer
Radiation source: fine-focus sealed tube graphite
Detector resolution: 8.3333 pixels $\mathrm{mm}^{-1}$
$\omega$ and $\varphi$ scans

4304 independent reflections
3726 reflections with $I>2 \sigma(I)$
$R_{\text {int }}=0.028$
$\theta_{\text {max }}=52.4^{\circ}, \theta_{\text {min }}=4.5^{\circ}$
$h=-17 \rightarrow 20$

Absorption correction: multi-scan
(SADABS; Bruker, 2008)
$T_{\text {min }}=0.155, T_{\text {max }}=0.205$
18034 measured reflections

## Refinement

Refinement on $F^{2}$
Least-squares matrix: full
$R\left[F^{2}>2 \sigma\left(F^{2}\right)\right]=0.021$
$w R\left(F^{2}\right)=0.046$
$S=1.07$
4304 reflections
62 parameters
0 restraints
$k=-12 \rightarrow 10$
$l=-30 \rightarrow 28$

Primary atom site location: structure-invariant direct methods
Secondary atom site location: difference Fourier map
$w=1 /\left[\sigma^{2}\left(F_{\mathrm{o}}{ }^{2}\right)+(0.0176 P)^{2}+0.4317 P\right]$
where $P=\left(F_{\mathrm{o}}^{2}+2 F_{\mathrm{c}}^{2}\right) / 3$
$(\Delta / \sigma)_{\max }=0.004$
$\Delta \rho_{\max }=1.59 \mathrm{e}^{-3}$
$\Delta \rho_{\min }=-1.99$ e $\AA^{-3}$
Extinction correction: SHELXL97 (Sheldrick, 2008),
$\mathrm{Fc}^{*}=\mathrm{kFc}\left[1+0.001 \mathrm{xFc}^{2} \lambda^{3} / \sin (2 \theta)\right]^{-1 / 4}$
Extinction coefficient: 0.0075 (2)

## Special details

Geometry. All e.s.d.'s (except the e.s.d. in the dihedral angle between two 1.s. planes) are estimated using the full covariance matrix. The cell e.s.d.'s are taken into account individually in the estimation of e.s.d.'s in distances, angles and torsion angles; correlations between e.s.d.'s in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell e.s.d.'s is used for estimating e.s.d.'s involving 1.s. planes.
Refinement. Refinement of $F^{2}$ against ALL reflections. The weighted $R$-factor $w R$ and goodness of fit $S$ are based on $F^{2}$, conventional $R$-factors $R$ are based on $F$, with $F$ set to zero for negative $F^{2}$. The threshold expression of $F^{2}>\sigma\left(F^{2}\right)$ is used only for calculating $R$ factors(gt) etc. and is not relevant to the choice of reflections for refinement. $R$-factors based on $F^{2}$ are statistically about twice as large as those based on $F$, and $R$ - factors based on ALL data will be even larger.

Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters ( $A^{2}$ )

|  | $x$ | $y$ | $z$ | $U_{\text {iso }} * / U_{\text {eq }}$ |
| :--- | :--- | :--- | :--- | :--- |
| Ba1 | $0.159652(9)$ | 0.2500 | $0.744870(6)$ | $0.00801(2)$ |
| Ba 2 | $0.138138(9)$ | 0.2500 | $0.417071(6)$ | $0.00841(2)$ |
| P 1 | $-0.04603(4)$ | -0.2500 | $0.81569(3)$ | $0.00724(6)$ |
| P2 | $-0.28072(4)$ | -0.2500 | $0.95778(3)$ | $0.00722(6)$ |
| O1 | $-0.11642(14)$ | -0.2500 | $0.92264(9)$ | $0.0129(2)$ |
| O2 | $-0.09496(10)$ | $-0.0264(2)$ | $0.76295(7)$ | $0.01169(13)$ |
| O3 | $-0.35537(10)$ | $-0.0271(2)$ | $0.91982(6)$ | $0.01215(14)$ |
| O4 | $-0.27382(15)$ | -0.2500 | $0.06760(9)$ | $0.0130(2)$ |
| O5 | $0.11429(14)$ | -0.2500 | $0.83242(11)$ | $0.0160(3)$ |

Atomic displacement parameters $\left(A^{2}\right)$

|  | $U^{11}$ | $U^{22}$ | $U^{33}$ | $U^{12}$ | $U^{13}$ | $U^{23}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Ba 1 | $0.00795(3)$ | $0.00736(4)$ | $0.00873(3)$ | 0.000 | $-0.00047(2)$ | 0.000 |


|  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Ba2 | $0.00856(3)$ | $0.00891(4)$ | $0.00776(3)$ | 0.000 | $0.00084(2)$ | 0.000 |
| P1 | $0.00544(11)$ | $0.00757(16)$ | $0.00873(13)$ | 0.000 | $0.00010(9)$ | 0.000 |
| P2 | $0.00839(12)$ | $0.00706(16)$ | $0.00622(12)$ | 0.000 | $0.00066(9)$ | 0.000 |
| O1 | $0.0088(4)$ | $0.0198(7)$ | $0.0100(4)$ | 0.000 | $0.0012(3)$ | 0.000 |
| O2 | $0.0126(3)$ | $0.0091(4)$ | $0.0133(3)$ | $0.0008(3)$ | $0.0005(2)$ | $0.0022(3)$ |
| O3 | $0.0145(3)$ | $0.0101(4)$ | $0.0119(3)$ | $0.0029(3)$ | $0.0000(2)$ | $0.0022(3)$ |
| O4 | $0.0161(5)$ | $0.0160(6)$ | $0.0069(4)$ | 0.000 | $0.0003(3)$ | 0.000 |
| O5 | $0.0061(3)$ | $0.0243(8)$ | $0.0176(5)$ | 0.000 | $-0.0008(3)$ | 0.000 |

## Geometric parameters ( $\AA,^{\circ}$ )

| $\mathrm{Ba}-\mathrm{O} 3{ }^{\text {i }}$ | 2.7585 (10) |
| :---: | :---: |
| $\mathrm{Ba}-\mathrm{O} 3^{\text {ii }}$ | 2.7585 (10) |
| $\mathrm{Ba} 1-\mathrm{O} 2{ }^{\text {ii }}$ | 2.7591 (10) |
| $\mathrm{Ba} 1-\mathrm{O} 2{ }^{\text {i }}$ | 2.7591 (10) |
| $\mathrm{Ba}-\mathrm{O} 4^{\text {iii }}$ | 2.7978 (13) |
| Ba1-O2 | 2.8392 (10) |
| $\mathrm{Ba}-\mathrm{O} 2{ }^{\text {iv }}$ | 2.8392 (10) |
| $\mathrm{Ba} 1-\mathrm{O} 5^{\text {v }}$ | 3.0850 (6) |
| Ba1-O5 | 3.0850 (6) |
| $\mathrm{Ba} 2-\mathrm{O} 5^{\mathrm{vi}}$ | 2.5794 (13) |
| $\mathrm{Ba} 2-\mathrm{O} 3^{\mathrm{ii}}$ | 2.7377 (10) |
| $\mathrm{Ba} 2-\mathrm{O} 3{ }^{\text {i }}$ | 2.7377 (10) |
| $\mathrm{Ba} 2-\mathrm{O} 2^{\text {iii }}$ | 2.8133 (10) |
| $\mathrm{Ba} 2-\mathrm{O} 2^{\text {vii }}$ | 2.8133 (10) |
| $\mathrm{Ba} 2-\mathrm{O} 3{ }^{\text {viii }}$ | 2.9094 (10) |
| $\mathrm{Ba} 2-\mathrm{O} 3^{\text {ix }}$ | 2.9094 (10) |
| $\mathrm{Ba} 2-\mathrm{O} 4^{\mathrm{x}}$ | 2.9313 (4) |
| $\mathrm{Ba} 2-\mathrm{O} 4^{\mathrm{xi}}$ | 2.9313 (4) |
| $\mathrm{Ba} 2-\mathrm{P} 1^{\text {iii }}$ | 3.3255 (4) |
| $\mathrm{Ba} 2-\mathrm{P} 2{ }^{\text {viii }}$ | 3.3668 (4) |
| $\mathrm{Ba} 2-\mathrm{P} 2^{\text {xii }}$ | 3.3812 (2) |
| P1-O5 | 1.5067 (13) |
| $\mathrm{O} 3{ }^{\mathrm{i}}-\mathrm{Ba} 1-\mathrm{O} 3^{\mathrm{ii}}$ | 68.66 (5) |
| $\mathrm{O} 3{ }^{\mathrm{i}}-\mathrm{Ba} 1-\mathrm{O} 2^{\mathrm{ii}}$ | 109.06 (3) |
| $\mathrm{O} 3{ }^{\text {iii }}-\mathrm{Ba} 1-\mathrm{O} 2^{\text {ii }}$ | 72.09 (3) |
| $\mathrm{O} 3{ }^{\mathrm{i}}-\mathrm{Ba} 1-\mathrm{O} 2^{\text {i }}$ | 72.09 (3) |
| $\mathrm{O} 3{ }^{\text {iii }}-\mathrm{Ba} 1-\mathrm{O} 2^{\mathrm{i}}$ | 109.06 (3) |
| $\mathrm{O} 2{ }^{\text {ii }}-\mathrm{Ba} 1-\mathrm{O} 2^{\mathrm{i}}$ | 68.43 (4) |
| $\mathrm{O} 3^{\mathrm{i}}-\mathrm{Ba} 1-\mathrm{O} 4^{\text {iii }}$ | 141.44 (2) |
| $\mathrm{O} 3{ }^{\text {iii }}-\mathrm{Ba} 1-\mathrm{O} 4{ }^{\text {iii }}$ | 141.44 (3) |
| $\mathrm{O} 2{ }^{\text {ii }}-\mathrm{Ba} 1-\mathrm{O} 4{ }^{\text {iii }}$ | 73.93 (3) |


| $\mathrm{P} 1-\mathrm{O} 2^{\text {xiii }}$ | 1.5208 (11) |
| :---: | :---: |
| $\mathrm{P} 1-\mathrm{O} 2$ | 1.5208 (11) |
| P1-O1 | 1.6148 (13) |
| P 1 -Ba2 ${ }^{\text {iii }}$ | 3.3255 (4) |
| $\mathrm{P} 2-\mathrm{O} 4^{\text {xiv }}$ | 1.5175 (13) |
| $\mathrm{P} 2-\mathrm{O} 3^{\text {xiii }}$ | 1.5236 (11) |
| P2-O3 | 1.5236 (11) |
| P2-O1 | 1.6012 (14) |
| $\mathrm{P} 2-\mathrm{Ba} 2^{\mathrm{xv}}$ | 3.3668 (4) |
| $\mathrm{P} 2-\mathrm{Ba} 2^{\mathrm{xvi}}$ | 3.3812 (2) |
| $\mathrm{P} 2-\mathrm{Ba} 2^{\mathrm{xvii}}$ | 3.3812 (2) |
| $\mathrm{O} 2-\mathrm{Ba} 1^{\mathrm{xvi}}$ | 2.7591 (10) |
| $\mathrm{O} 2-\mathrm{Ba} 2{ }^{\text {iii }}$ | 2.8133 (10) |
| $\mathrm{O} 3-\mathrm{Ba} 2^{\mathrm{xvi}}$ | 2.7377 (10) |
| $\mathrm{O} 3-\mathrm{Ba} 1^{\mathrm{xvi}}$ | 2.7585 (10) |
| $\mathrm{O} 3-\mathrm{Ba} 2{ }^{\mathrm{xv}}$ | 2.9094 (10) |
| $\mathrm{O} 4-\mathrm{P} 2^{\mathrm{xviii}}$ | 1.5175 (13) |
| $\mathrm{O} 4-\mathrm{Ba} 1^{\text {iii }}$ | 2.7978 (13) |
| $\mathrm{O} 4-\mathrm{Ba} 2{ }^{\text {xix }}$ | 2.9313 (4) |
| $\mathrm{O} 4-\mathrm{Ba} 2^{\mathrm{xx}}$ | 2.9313 (4) |
| O5-Ba2 ${ }^{\text {xxi }}$ | 2.5794 (13) |
| O5-Ba1 ${ }^{\text {xxii }}$ | 3.0850 (6) |
| $\mathrm{O} 3{ }^{\text {ii }}-\mathrm{Ba} 2-\mathrm{O} 3{ }^{\text {ix }}$ | 76.39 (3) |
| $\mathrm{O} 3-\mathrm{Ba} 2-\mathrm{O} 3^{\text {ix }}$ | 104.688 (19) |
| $\mathrm{O} 2{ }^{\text {iiii }}-\mathrm{Ba} 2-\mathrm{O} 3^{\text {ix }}$ | 94.29 (3) |
| $\mathrm{O} 2{ }^{\text {vii }}-\mathrm{Ba} 2-\mathrm{O} 3{ }^{\text {ix }}$ | 71.99 (3) |
| $\mathrm{O} 3{ }^{\text {viii }}-\mathrm{Ba} 2-\mathrm{O} 3{ }^{\text {ix }}$ | 50.95 (4) |
| $\mathrm{O} 5^{\text {vi }}-\mathrm{Ba} 2-\mathrm{O} 4^{\mathrm{x}}$ | 77.53 (3) |
| $\mathrm{O} 3{ }^{\text {iii }}-\mathrm{Ba} 2-\mathrm{O} 4^{\mathrm{x}}$ | 52.44 (3) |
| $\mathrm{O} 3{ }^{\mathrm{i}}-\mathrm{Ba} 2-\mathrm{O} 4^{\mathrm{x}}$ | 118.59 (3) |
| $\mathrm{O} 2{ }^{\text {iii }}-\mathrm{Ba} 2-\mathrm{O} 4^{\text {x }}$ | 122.07 (3) |

## sup-4

| $\mathrm{O} 2{ }^{\mathrm{i}}-\mathrm{Ba} 1-\mathrm{O} 4^{\text {iii }}$ |
| :---: |
| $\mathrm{O} 3{ }^{\mathrm{i}}-\mathrm{Ba} 1-\mathrm{O} 2$ |
| $\mathrm{O} 3{ }^{\mathrm{ii}}-\mathrm{Ba} 1-\mathrm{O} 2$ |
| $\mathrm{O} 2 \mathrm{ii}-\mathrm{Ba} 1-\mathrm{O} 2$ |
| $\mathrm{O} 2{ }^{\mathrm{i}}-\mathrm{Ba} 1-\mathrm{O} 2$ |
| $\mathrm{O} 4{ }^{\mathrm{iii}}-\mathrm{Ba} 1-\mathrm{O} 2$ |
| $\mathrm{O} 3{ }^{\mathrm{i}}-\mathrm{Ba} 1-\mathrm{O} 2^{\text {iv }}$ |
| $\mathrm{O} 3{ }^{\text {ii }}-\mathrm{Ba} 1-\mathrm{O} 2{ }^{\text {iv }}$ |
| $\mathrm{O} 22^{\mathrm{ii}}-\mathrm{Ba}-\mathrm{O}^{\text {iv }}$ |
| $\mathrm{O} 2{ }^{\text {i }}-\mathrm{Ba} 1-\mathrm{O} 2^{\text {iv }}$ |
| $\mathrm{O} 4^{\mathrm{iii}}-\mathrm{Ba} 1-\mathrm{O} 2^{\text {iv }}$ |
| $\mathrm{O} 2-\mathrm{Ba} 1-\mathrm{O} 2{ }^{\text {iv }}$ |
| $\mathrm{O} 3{ }^{\mathrm{i}}-\mathrm{Ba} 1-\mathrm{O} 5^{\mathrm{v}}$ |
| $\mathrm{O} 3{ }^{\text {iii }}-\mathrm{Ba} 1-\mathrm{O} 5^{\mathrm{v}}$ |
| $\mathrm{O} 2{ }^{\text {iii }}-\mathrm{Ba} 1-\mathrm{O} 5^{\text {v }}$ |
| $\mathrm{O} 2{ }^{\mathrm{i}}-\mathrm{Ba} 1-\mathrm{O} 5^{\mathrm{v}}$ |
| $\mathrm{O} 4^{\mathrm{iii}}-\mathrm{Ba} 1-\mathrm{O} 5^{\mathrm{v}}$ |
| $\mathrm{O} 2-\mathrm{Ba} 1-\mathrm{O}^{\mathrm{v}}$ |
| $\mathrm{O} 2{ }^{\text {iv }}-\mathrm{Ba} 1-\mathrm{O} 5^{\text {v }}$ |
| $\mathrm{O} 3{ }^{\text {i }}-\mathrm{Ba} 1-\mathrm{O} 5$ |
| $\mathrm{O} 3{ }^{\text {ii }}-\mathrm{Ba} 1-\mathrm{O} 5$ |
| $\mathrm{O} 2{ }^{\mathrm{ii}}-\mathrm{Ba} 1-\mathrm{O} 5$ |
| $\mathrm{O} 2{ }^{\mathrm{i}}-\mathrm{Ba} 1-\mathrm{O} 5$ |
| $\mathrm{O} 4{ }^{\mathrm{iii}}-\mathrm{Ba} 1-\mathrm{O} 5$ |
| $\mathrm{O} 2-\mathrm{Ba}-\mathrm{O} 5$ |
| $\mathrm{O} 2{ }^{\text {iv }}-\mathrm{Ba} 1-\mathrm{O} 5$ |
| $\mathrm{O} 5{ }^{\mathrm{v}}-\mathrm{Ba} 1-\mathrm{O} 5$ |
| $\mathrm{O} 5^{\mathrm{vi}}-\mathrm{Ba} 2-\mathrm{O} 3{ }^{\text {ii }}$ |
| $\mathrm{O} 5^{\mathrm{vi}}-\mathrm{Ba} 2-\mathrm{O} 3^{\text {i }}$ |
| $\mathrm{O} 3{ }^{\text {iii }}-\mathrm{Ba} 2-\mathrm{O} 3{ }^{\text {i }}$ |
| $\mathrm{O} 5^{\mathrm{vi}}-\mathrm{Ba} 2-\mathrm{O} 2{ }^{\text {iii }}$ |
| $\mathrm{O} 3{ }^{\text {iii }}-\mathrm{Ba} 2-\mathrm{O} 2{ }^{\text {iii }}$ |
| $\mathrm{O} 3{ }^{\text {i }}-\mathrm{Ba} 2-\mathrm{O} 2^{\text {iii }}$ |
| $\mathrm{O} 5^{\mathrm{vi}}-\mathrm{Ba} 2-\mathrm{O} 2{ }^{\text {vii }}$ |
| $\mathrm{O} 3{ }^{\text {ii }}-\mathrm{Ba} 2-\mathrm{O} 2^{\mathrm{vii}}$ |
| $\mathrm{O} 3-\mathrm{Ba} 2-\mathrm{O} 2^{\text {vii }}$ |
| $\mathrm{O} 2{ }^{\text {iii }}-\mathrm{Ba} 2-\mathrm{O} 2 \mathrm{Vii}^{\text {vii }}$ |
| $\mathrm{O} 5{ }^{\text {vi }}-\mathrm{Ba} 2-\mathrm{O} 3^{\text {viii }}$ |
| $\mathrm{O} 3{ }^{\text {iii }}-\mathrm{Ba} 2-\mathrm{O} 3^{\text {viii }}$ |
| $\mathrm{O} 3{ }^{\text {i }}-\mathrm{Ba} 2-\mathrm{O} 3{ }^{\text {viii }}$ |
| $\mathrm{O} 2{ }^{\text {iii }}-\mathrm{Ba} 2-\mathrm{O} 3^{\text {viii }}$ |

73.93 (3)
73.87 (3)
109.79 (3)
177.035 (6)
112.59 (4)
103.55 (3)
109.79 (3)
73.87 (3)
112.59 (4)
177.035 (6)
103.55 (3)
66.25 (4)
146.01 (3)
78.63 (3)
67.45 (3)
129.77 (3)
71.89 (3)
110.43 (3)
49.81 (3)
78.63 (3)
146.01 (3)
129.77 (3)
67.45 (3)
71.89 (3)
49.81 (3)
110.43 (3)
130.97 (5)
110.68 (3)
110.68 (3)
69.25 (4)
74.14 (3)
169.56 (3)
118.44 (3)
74.14 (3)
118.44 (3)
169.56 (3)
53.01 (4)
144.15 (3)
104.688 (19)
76.39 (3)
71.99 (3)
$\mathrm{O} 2^{\text {vii }}-\mathrm{Ba} 2-\mathrm{O} 4^{\mathrm{x}}$
$\mathrm{O} 3^{\text {viii }}-\mathrm{Ba} 2-\mathrm{O}^{\mathrm{x}}$
$\mathrm{O} 3^{\mathrm{ix}}-\mathrm{Ba} 2-\mathrm{O} 4^{\mathrm{x}}$
$\mathrm{O} 5^{\mathrm{vi}}-\mathrm{Ba} 2-\mathrm{O} 4^{\mathrm{xi}}$
$\mathrm{O} 3^{\mathrm{ii}}-\mathrm{Ba} 2-\mathrm{O} 4^{\mathrm{xi}}$
$\mathrm{O} 3^{\mathrm{i}}-\mathrm{Ba} 2-\mathrm{O} 4^{\mathrm{xi}}$
$\mathrm{O} 2^{\mathrm{iii}}-\mathrm{Ba} 2-\mathrm{O} 4^{\mathrm{xi}}$
$\mathrm{O} 2{ }^{\text {vii }}-\mathrm{Ba} 2-\mathrm{O} 4^{\mathrm{xi}}$
$\mathrm{O}^{\text {viii }}-\mathrm{Ba} 2-\mathrm{O} 4^{\text {xi }}$
$\mathrm{O} 3^{\mathrm{ix}}-\mathrm{Ba} 2-\mathrm{O} 4^{\mathrm{xi}}$
$\mathrm{O} 4^{\mathrm{x}}-\mathrm{Ba} 2-\mathrm{O} 4^{\mathrm{xi}}$
$\mathrm{O} 5-\mathrm{P} 1-\mathrm{O} 2^{\text {xiii }}$
$\mathrm{O} 5-\mathrm{P} 1-\mathrm{O} 2$
$\mathrm{O} 2^{\text {xiii }}-\mathrm{P} 1-\mathrm{O} 2$
O5-P1-O1
$\mathrm{O} 2^{\mathrm{xiii}}-\mathrm{P} 1-\mathrm{O} 1$
$\mathrm{O} 2-\mathrm{P} 1-\mathrm{O} 1$
P2-O1-P1
$\mathrm{P} 1-\mathrm{O} 2-\mathrm{Ba} 1^{\mathrm{xvi}}$
$\mathrm{P} 1-\mathrm{O} 2-\mathrm{Ba} 2{ }^{\mathrm{iii}}$
$\mathrm{Ba} 1^{\mathrm{xvi}}-\mathrm{O} 2-\mathrm{Ba} 2^{\text {iii }}$
P1-O2-Ba1
$\mathrm{Ba} 1^{\mathrm{xvi}}-\mathrm{O} 2-\mathrm{Ba} 1$
$\mathrm{Ba} 2^{\mathrm{iii}}-\mathrm{O} 2-\mathrm{Ba} 1$
$\mathrm{P} 2-\mathrm{O} 3-\mathrm{Ba} 2^{\mathrm{xvi}}$
$\mathrm{P} 2-\mathrm{O} 3-\mathrm{Ba} 1^{\mathrm{xvi}}$
$\mathrm{Ba} 2^{\mathrm{xvi}}-\mathrm{O} 3-\mathrm{Ba} 1^{\mathrm{xvi}}$
$\mathrm{P} 2-\mathrm{O} 3-\mathrm{Ba}^{\mathrm{xv}}$
$\mathrm{Ba} 2^{\mathrm{xvi}}-\mathrm{O} 3-\mathrm{Ba} 2^{\mathrm{xv}}$
$\mathrm{Ba} 1^{\mathrm{xvi}}-\mathrm{O} 3-\mathrm{Ba} 2^{\mathrm{xv}}$
$\mathrm{P} 2^{\text {xviii- }} 04-\mathrm{Ba} 1^{i i i}$
$\mathrm{P} 2^{\mathrm{xviii}}-\mathrm{O} 4-\mathrm{Ba} 2^{\mathrm{xix}}$
$\mathrm{Ba} 1^{\mathrm{iii}}-\mathrm{O} 4-\mathrm{Ba} 2^{\mathrm{xix}}$
$\mathrm{P} 2^{\mathrm{xviii}}-\mathrm{O} 4-\mathrm{Ba} 2^{\mathrm{xx}}$
$\mathrm{Ba} 1^{\mathrm{iii}}-\mathrm{O} 4-\mathrm{Ba}^{2 \mathrm{xx}}$
$\mathrm{Ba} 2^{\mathrm{xix}}-\mathrm{O} 4-\mathrm{Ba}^{\mathrm{xx}}$
$\mathrm{P} 1-\mathrm{O} 5-\mathrm{Ba} 2^{\mathrm{xxi}}$
P1-O5-Ba1 ${ }^{x x i i}$
$\mathrm{Ba} 2^{\mathrm{xxi}}-\mathrm{O} 5-\mathrm{Ba}^{\mathrm{xxii}}$
P1-O5-Ba1
$\mathrm{Ba} 2^{\mathrm{xxi}}-\mathrm{O} 5-\mathrm{Ba} 1$
71.11 (3)
131.51 (3)
80.73 (3)
77.53 (3)
118.59 (3)
52.44 (3)
71.11 (3)
122.07 (3)
80.73 (3)
131.51 (3)
146.51 (5)
111.63 (5)
111.63 (5)
111.29 (8)
105.06 (8)
108.47 (5)
108.47 (5)
131.52 (9)
136.86 (5)
95.57 (5)
95.66 (3)
104.14 (5)
112.16 (4)
106.55 (3)
101.17 (4)
136.36 (5)
111.02 (4)
93.55 (5)
103.61 (3)
106.11 (3)
160.15 (8)
93.46 (3)
92.23 (3)
93.46 (3)
92.23 (3)
146.51 (5)
161.87 (9)
94.30 (3)
93.20 (3)
94.30 (3)
93.20 (3)

## supplementary materials

| $\mathrm{O} 2^{\mathrm{vii}}-\mathrm{Ba} 2-\mathrm{O} 3^{\text {viii }}$ | 94.29 (3) | $\mathrm{Ba} 1^{\mathrm{xxii}}-\mathrm{O} 5-\mathrm{Ba} 1$ | 130.97 (5) |
| :---: | :---: | :---: | :---: |
| $\mathrm{O} 5^{\text {vi }}-\mathrm{Ba} 2-\mathrm{O} 3{ }^{\text {ix }}$ | 144.15 (3) |  |  |
| $\begin{aligned} & \text { Symmetry codes: (i) } \\ & 2 ; \text { (vii) }-x, y+1 / 2,-z \\ & y+1,-z+3 / 2 ;(\text { xiii) } x, \\ & z-1 ;(\text { (ix }) x-1 / 2, y-1 \end{aligned}$ | $\begin{aligned} & \text { ii) } x+1 / 2,-y \\ & -y, z-1 / 2 \text {; (ix } \\ & y, z+1 \text {; (xv) } \\ & 2, y,-z+1 / 2 \end{aligned}$ | $\begin{aligned} & \text { iii) }-x,-y,-z+1 \text {; (iv) } \\ & 2, z-1 / 2 ; \text { (x) } x+1 / 2, y \\ & 1 / 2 ;(\mathrm{xvi}) x-1 / 2, y,- \\ & -y, z+1 / 2 ;(\mathrm{xxii}) x, y \end{aligned}$ | $\begin{aligned} & +1, z ;(\mathrm{vi}) \\ & 2, y,-z+1 / \\ & -1,-z+3 / 2 \end{aligned}$ |

Fig. 1


Fig. 2


